

Thursday, April 8, 2021, 4:00 pm

COLLOQUIUM TALK

Speaker: **Liem Nguyen (Louisiana State University)**

Zoom Meeting (ID: 91520924644)

## Weil sum, Helleseth Conjectures, and Applications

### Abstract:

The Weil sum of an additive character  $\mu$  over a finite field  $F$  is defined to be  $W_{F,s}(a) = \sum_{x \in F} \mu(x^s - ax)$  where  $s$  is an integer coprime to  $|F^*|$ . The

Weil spectrum counts distinct values of the Weil sum as  $a$  runs through the invertible elements in the finite field. Determining the values of these sums and the size of its spectrum give answers to long-standing problems in communication networks, coding and information theory. In this talk, we prove a special case of the Vanishing Conjecture of Helleseth (1971) on the presence of zero in the Weil spectrum. We then propose a new conjecture on when the Weil spectrum contains at least five elements, and prove it for a certain class of Weil sum.